



TRIMM is supported by funding from the 7<sup>th</sup> Framework Programme Call: SST.2011.5.2-2.  
Theme: Advanced and cost effective road infrastructure construction, management and maintenance

# Cost Benefit of Monitoring

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TOMORROW'S ROAD INFRASTRUCTURE MONITORING AND MANAGEMENT

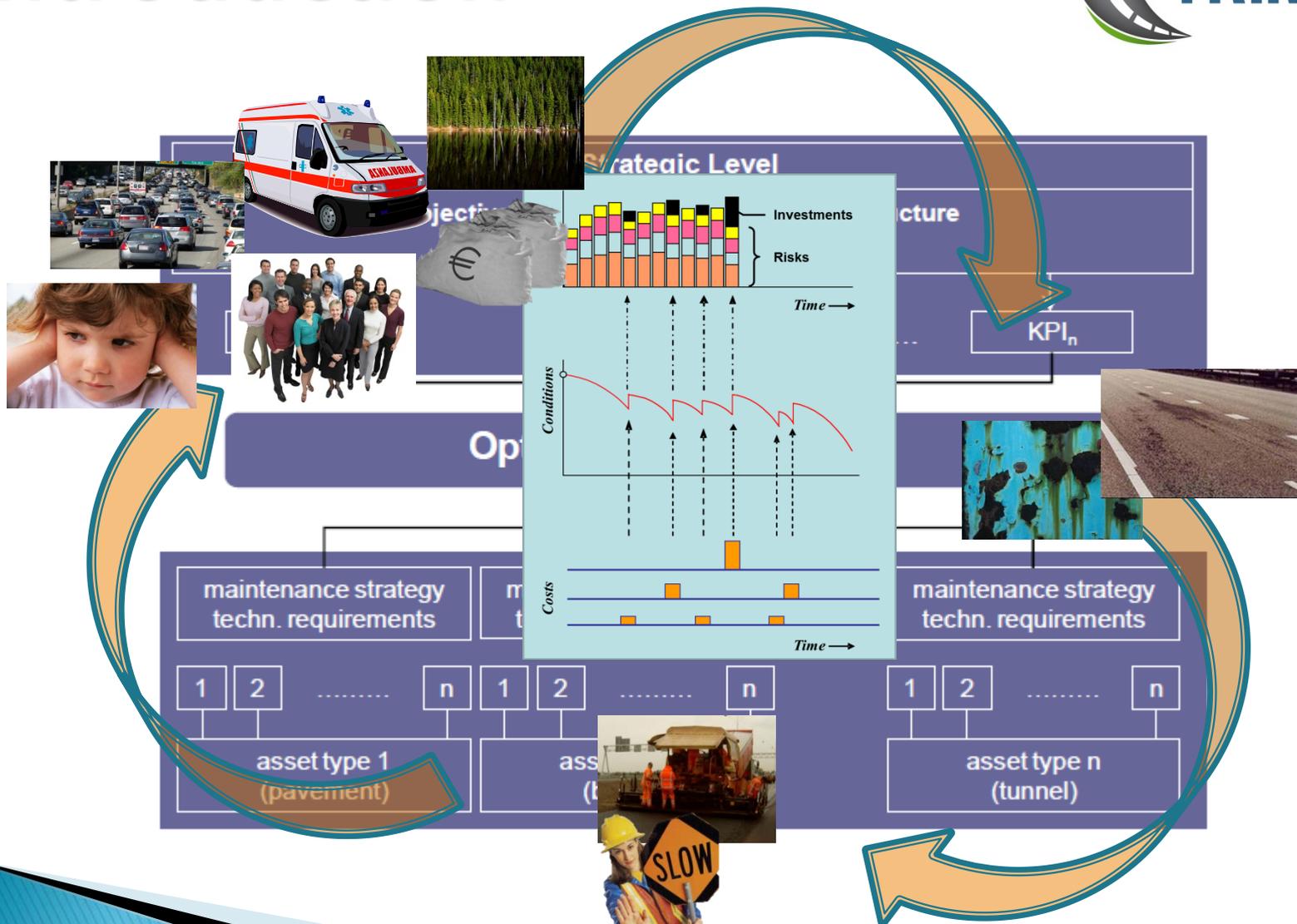
# Task



## ▶ Objective:

- **Develop SCBA model to assess life cycle costs and benefits of different maintenance scenarios – especially scenarios with different or without monitoring systems**
- Support decision making when designing monitoring schemes

# Introduction



TOMORROW'S ROAD INFRASTRUCTURE MONITORING & MANAGEMENT

# Introduction



## › EUSL

- Availability
- Safety
- Environment
- ...

## › Condition

- Rutting
- Skid Resistance
- Longitudinal Evenness
- ...



## › Actions

- Do nothing
- Remixing
- Renewal



TOMORROW'S ROAD INFRASTRUCTURE MONITORING & MANAGEMENT

# Introduction



## › Costs

- Action related
- Condition related
- Penalty
- ...

denoted  
 $C_{a.user} \dots C_{c.env} \cdot C_q$

## › EUSL

- Availability
- Safety
- Environment
- ...

denoted  
 $X_1 \dots X_E$

$\Delta X_1 \dots \Delta X_E$

## › Condition

- Rutting
- Skid Resistance
- Longitudinal Evenness
- ...

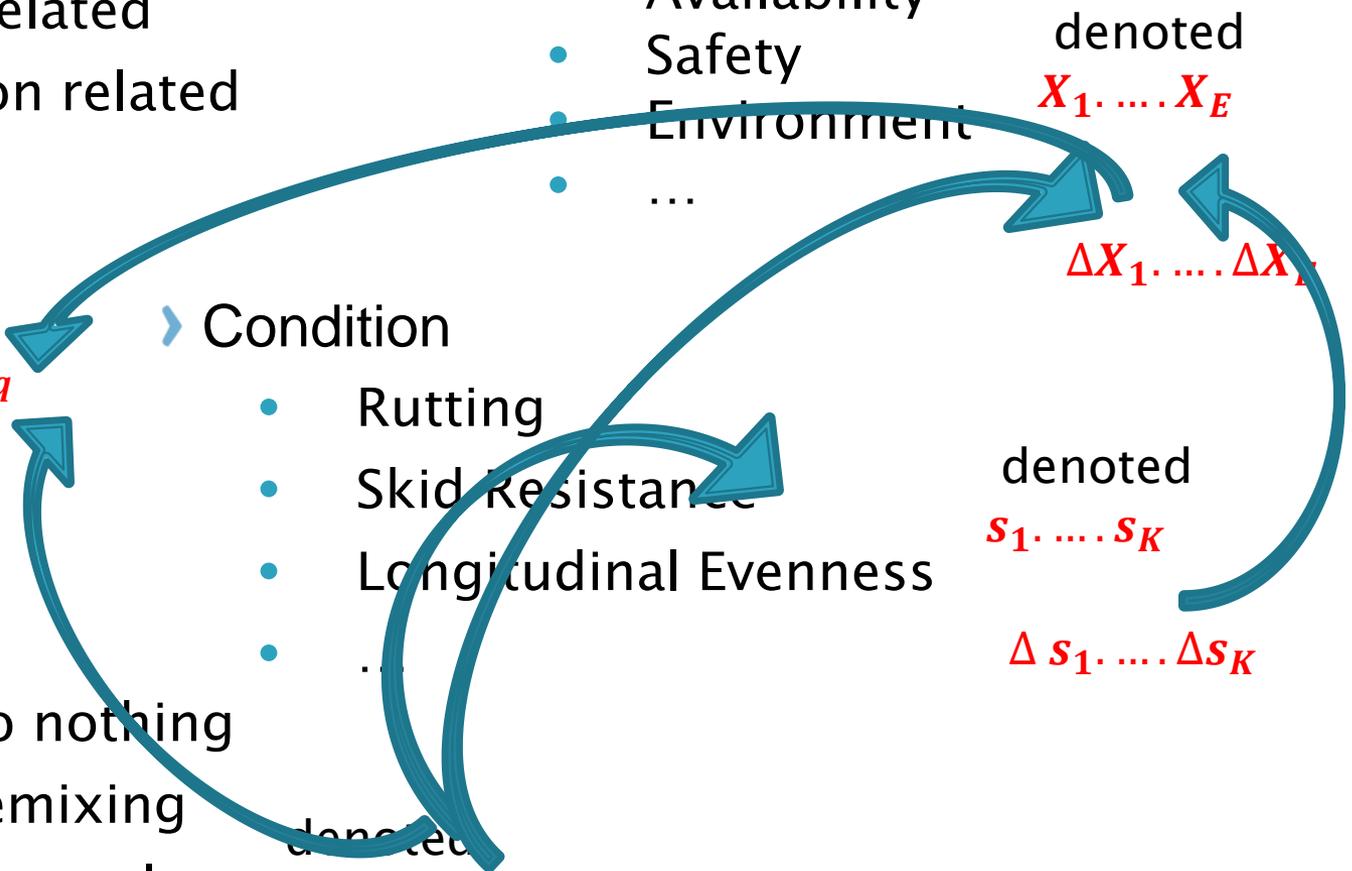
denoted  
 $S_1 \dots S_K$

$\Delta S_1 \dots \Delta S_K$

## › Actions

- Do nothing
- Remixing
- Renewal
- ...

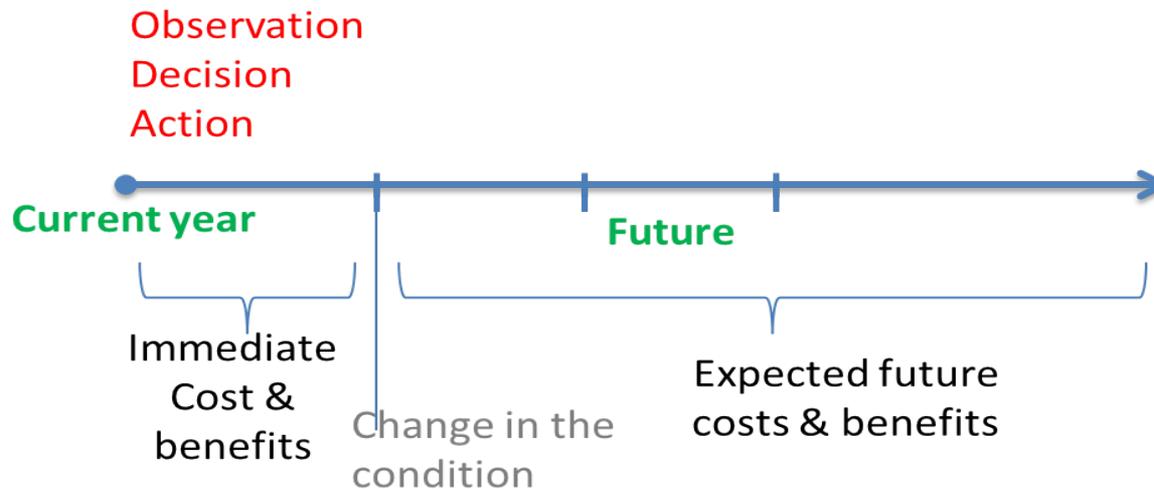
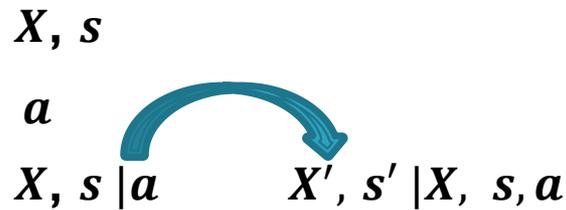
denoted  
 $a_0 \cdot a_1 \dots a_A$



# Problem description



$X$  EUSL  
 $s$  Condition  
 $a$  Action



# Problem description



## SIMPLE EXAMPLE

what can/will happen (see figure)  
when we have:

Repetitive decision periods  
decision at beginning of period  
e.g. each year

### 2 Actions

a repair  
 $\bar{a}$  do nothing

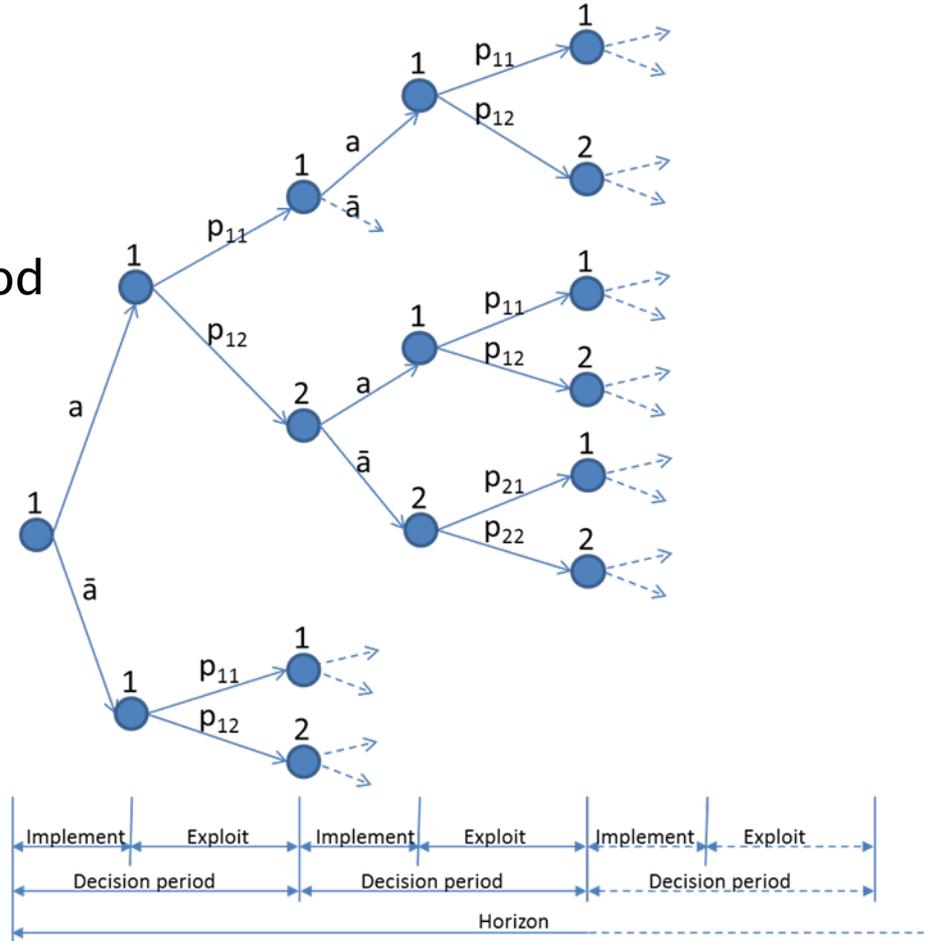
### 2 States (conditions)

1 good  
2 bad

### Degradation

Transition probabilities

$p_{ij}$  probability to change from state  $i$  to state  $j$  within a period

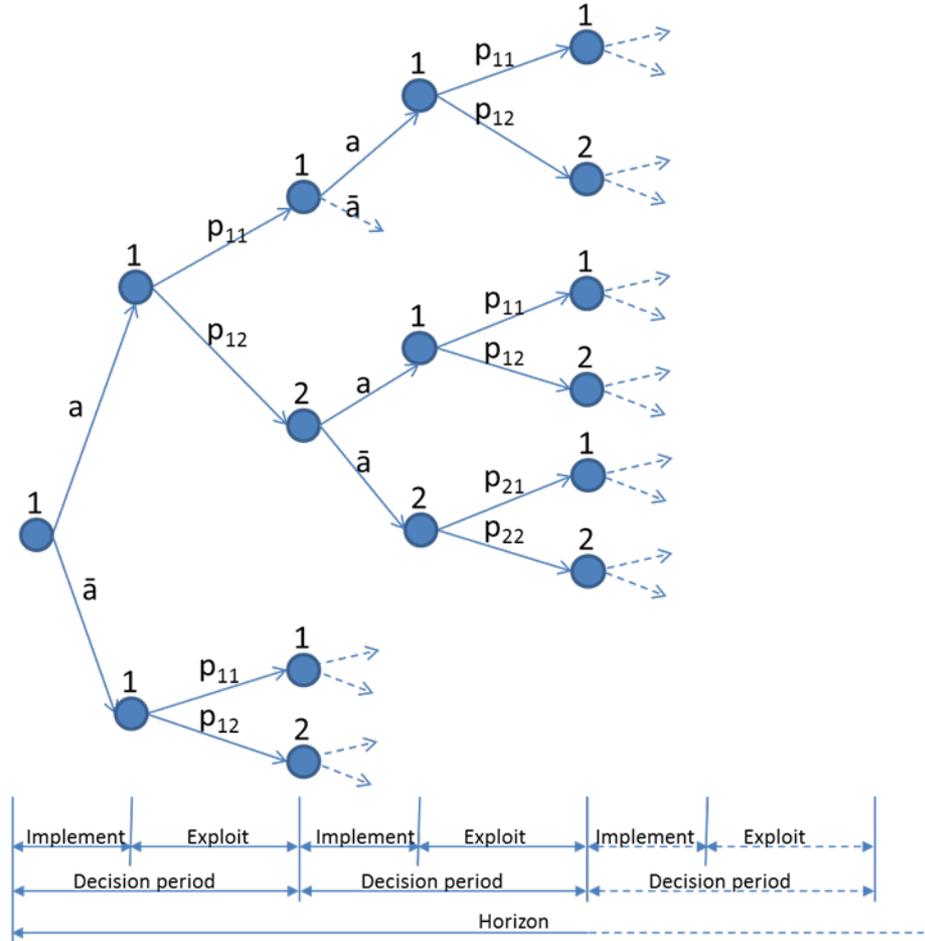
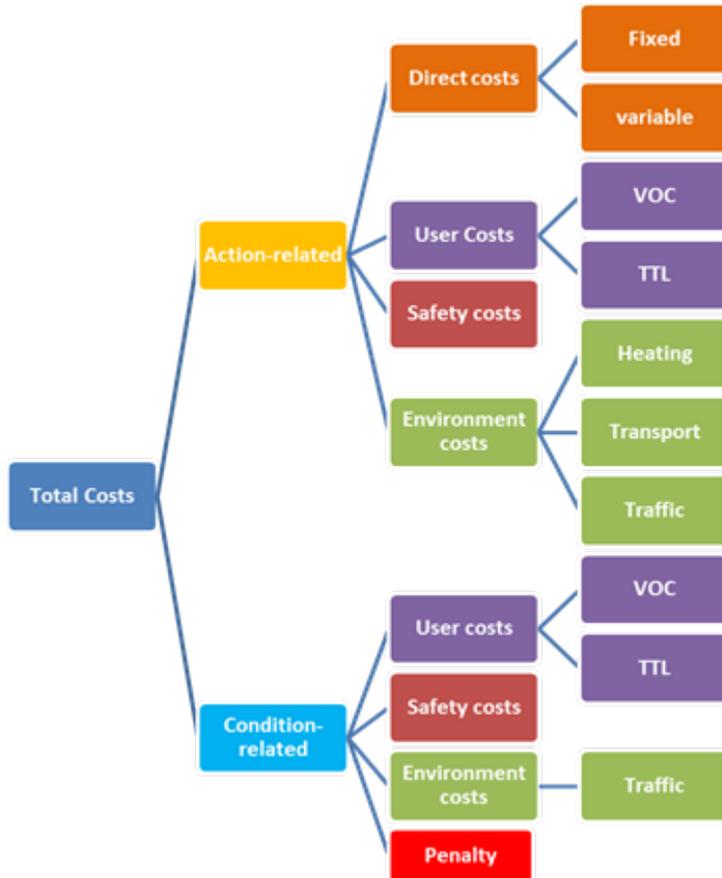


# Problem description



## SIMPLE EXAMPLE

what implications would this have



# Cost Benefit Analysis



## SIMPLE EXAMPLE Planning/decisions

Noting the repetitive character of the branches, we get

$$V(s) = C_{implement}(a) + \sum_{s' \in S} p_{s_a s'}^a (C_{exploit}(s_a, s') + \lambda V(s'))$$

$s$  condition at beginning of period

$s'$  condition at end of period

$s_a$  condition as a result of the action

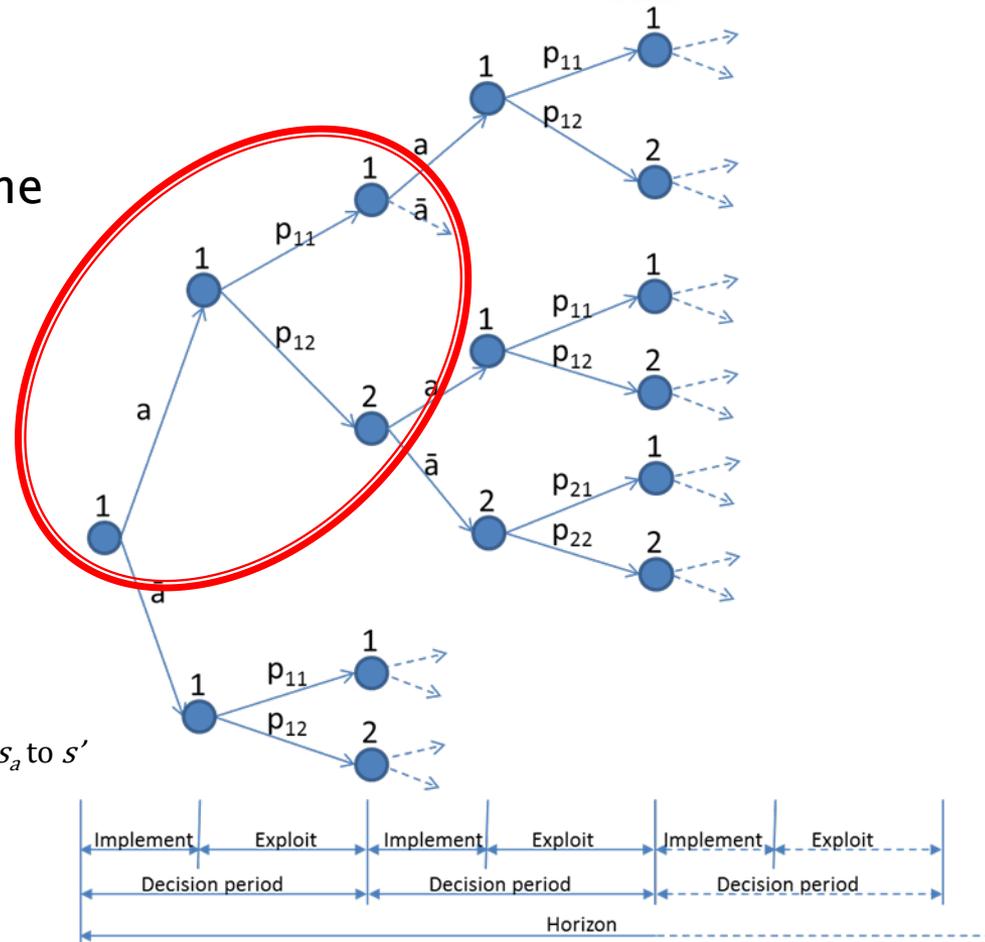
$\lambda$  discount for future costs

$p_{s_a s'}^a$  transition probability (after action  $a$ ) to move from state  $s_a$  to  $s'$

$V(s)$  cost associated with a node from the tree

$C_{exploit}(s_a, s')$  costs (risk) of exploitation

$C_{implement}(a)$  costs of implementing an action  $a$



Which enables cost optimisation and maintenance scenarios

# Cost Benefit Analysis



## Markov Decision Proces (MDP)

$$C^{a^*}(X, s, \hat{a}) = \min_{a=a_0, a_1, \dots, a_A} C_{action}(a, l) + C_{ind\_action}(a(s))$$

$$+ \sum_{X's'} P_{X's'}^{\hat{a}'} \left( C_{ind\_cond}(a, X, s, X', s') + C_q(a, X, s, X', s') + \lambda C^a(X', s', \hat{a}') \right)$$

$$V(s) = C_{implement}(a)$$

$$+ \sum_{s' \in S} p_{s_a s'}^a (C_{exploit}(s_a, s') + \lambda V(s'))$$

$s$  condition at beginning of period

$s'$  condition at end of period

$s_a$  condition as a result of the action

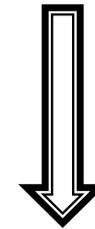
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$p_{s_a s'}^a$  transition probability (after action  $a$ ) to move from state  $s_a$  to  $s'$

$V(s)$  cost associated with a node from the tree

$C_{exploit}(s_a, s')$  costs (risk) of exploitation

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Planned strategy of actions

# Cost Benefit Analysis

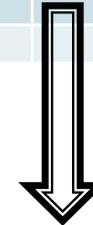


Year	Action	State before Action	State after Action	Monitoring Cost kEuro	Maint. Cost kEuro	EUSL Cost kEuro	Total Cost kEuro
1	DN	1	1	50	0	53.6	103.6
2	DN	1	1	2	0	53.6	55.6
3	DN	2	2	2	0	1092.4	1094.4
4	DN	2	2	2	0	1092.4	1094.4
5	DN	2	2	2	0	1092.4	1094.4
6	DN	2	2	2	0	1092.4	1094.4
7	R	3	1	2	12000	53.3	12055.3
8	DN	1	1	2	0	53.6	55.6
9	DN	1	1	2	0	53.6	55.6
10	DN	2	2	2	0	1092.4	1094.4



Net present Value

$$NPV = \sum_{t=1}^T \frac{B_t - C_t}{(1+r)^{t-1}}$$



Planned strategy of actions

# Monitoring



## Transition Matrices: States $s$

	1	2	3	4	5	6
1	0.85	0.15	0	0	0	0
2		0.7	0.3	0	0	0
3			0.5	0.5	0	0
4				0.4	0.6	0
5					0.55	0.45
6						1

$$P = \begin{bmatrix} p_{11} & \cdots & p_{1N} \\ \vdots & \ddots & \vdots \\ p_{N1} & \cdots & p_{NN} \end{bmatrix}$$

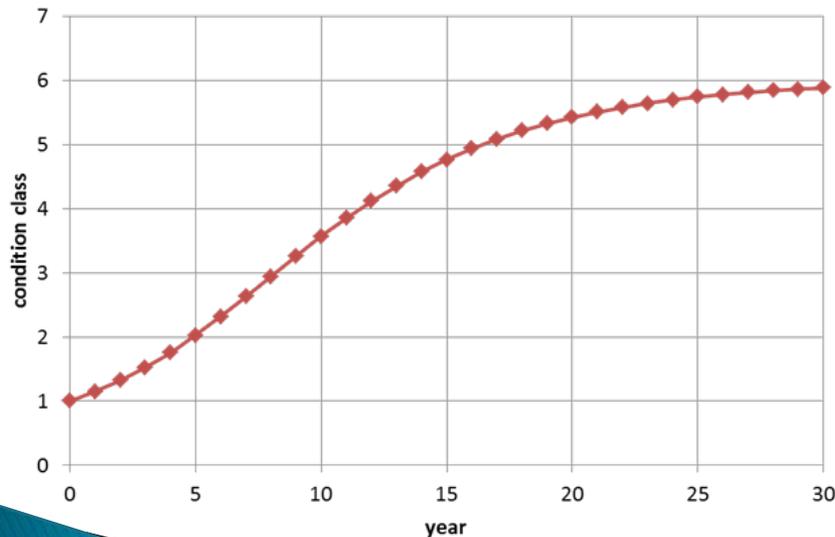
where  $p_{ij} = P\{s_{t+1} = j | s_t = i\}$

$$f_s(t) = (p_1 \dots \dots p_N)^T$$

with  $p_i = P\{s = i\}$

$$f_s(t + m) = (P^T)^m f_s(t)$$

Evolution of Average State value over years



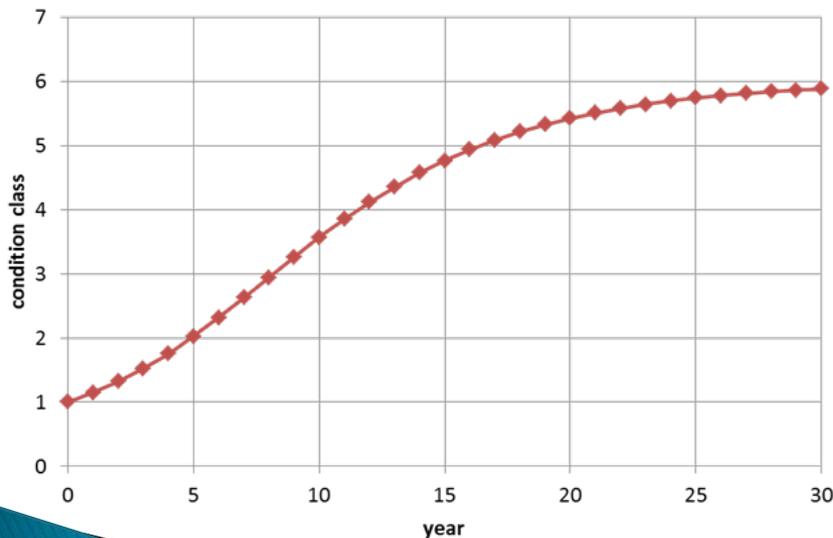
# Monitoring



## Measurements:

	1	2	3	4	5	6
1	0.85	0.15	0	0	0	0
2		0.7	0.3	0	0	0
3			0.5	0.5	0	0
4				0.4	0.6	0
5					0.55	0.45
6						1

Evolution of Average State value over years



Year $t$	$IRI_t$	Class $IRI_t$	Year $t + 1$	$IRI_{t+1}$	Class $IRI_{t+1}$	$\Delta IRI$
2003	0.843	1	2004	0.991	2	0.147
2004	0.991	2	2005	1.148	3	0.157
2005	1.148	3	2006	1.221	3	0.073
2006	1.221	3	2007	1.339	3	0.118
2007	1.339	3	2008	1.453	3	0.114
2008	1.453	3				

$$p_{ij} = \frac{n_{ij}}{n_i}$$

$n_{ij}$  is the number of transitions from state  $i$  to state  $j$  within a given time period and

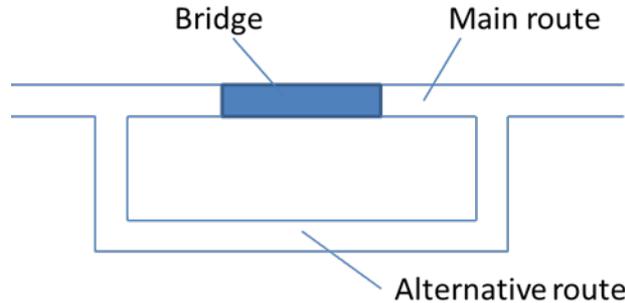
$n_i$  is the total number of elements in state  $i$  before the transition

TOMORROW'S ROAD INFRASTRUCTURE MONITORING & MANAGEMENT

# Cost Benefit Analysis



Example:



State  $s$  of bridge is monitored  
 Conservative upper bound is used for safety measures:

$$s^u = \mu(s) + \sigma(s)$$

When  $s^u$  exceeds the value of 3.30, heavy traffic is forced to take the alternative route, at a cost of 730 kEuro/year.

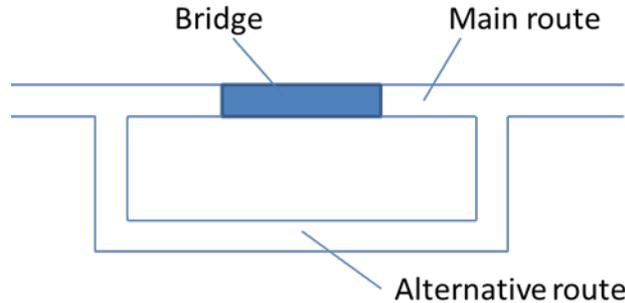
When  $s^u$  exceeds the value of 4.85, all traffic is forced to take the alternative route, which costs 3650 kEuro/year as a result of travel time loss

Description	value	unit
AADT passenger cars	4000	#/day
AADT trucks and lorries	1000	#/day
distance main route	10	km
distance alternative route	30	km
unit prize for TTL	10	Euro/h
Traffic speed $V$	100	km/h
Period	1	Year
Horizon	25	Year
discount rate	0.035	-
$\lambda$	0.9662	-
Criterion 1 for $f^u$	3.3	-
Criterion 2 for $f^u$	4.85	-
Action cost	120000	kEuro
Initial state	1	-
State after action	1	-

# Cost Benefit Analysis



Example:



## 2 Monitoring systems:

	1	2	3	4	5	6
1	0.859979	0.138306	0.000206	1.09E-05	0.000613	0.000885
2		0.751804	0.172779	0.027472	0.021391	0.026555
3			0.64749	0.235698	0.008101	0.108711
4				0.213994	0.007524	0.778481
5					0.105633	0.894367
6						1

### Reference system

50 kEuro initial cost  
2 kEuro annual cost

	1	2	3	4	5	6
1	0.85	0.15	0	0	0	0
2		0.7	0.3	0	0	0
3			0.5	0.5	0	0
4				0.4	0.6	0
5					0.55	0.45
6						1

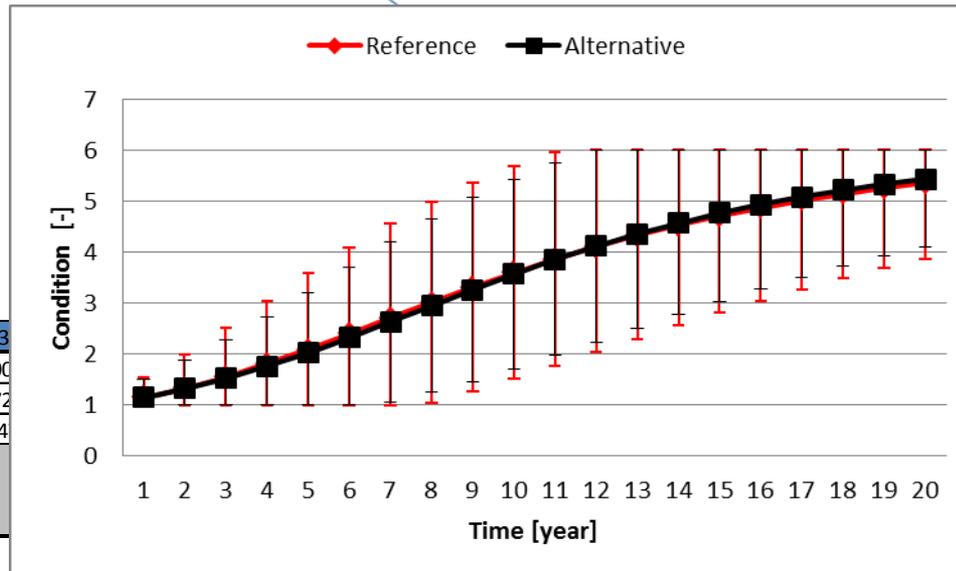
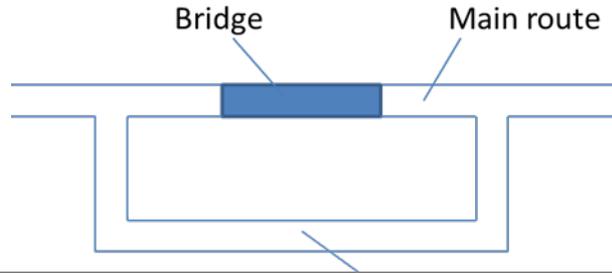
### Alternative system

100 kEuro initial cost  
4 kEuro annual cost

# Cost Benefit Analysis



Example:



	1	2	3
1	0.859979	0.138306	0.000
2		0.751804	0.172
3			0.64
4			
5			
6			

	4	5	6
4	0	0	0
5	0	0	0
6	0.5	0	0
7	0.4	0.6	0
8		0.55	0.45
9			1

Reference system

50 kEuro initial cost  
2 kEuro annual cost

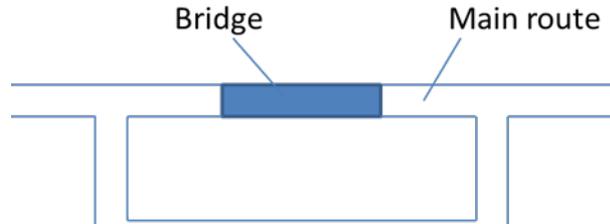
Alternative system

100 kEuro initial cost  
4 kEuro annual cost

# Cost Benefit Analysis



Example:



## Reference scenario

Year	Action	State before Action	State after Action	Monit. Cost kEuro	Maint. Cost kEuro	TTL Cost kEuro	Total Cost kEuro
1	DN	1	1	50	0	53.6	103.6
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11	DN	2	2	2	0	1092.4	1094.4
12	DN	2	2	2	0	1092.4	1094.4
13	DN	2	2	2	0	1092.4	1094.4
14	R	3	1	2	12000	53.3	12055.3
15	DN	1	1	2	0	53.6	55.6
16	DN	1	1	2	0	53.6	55.6
17	DN	2	2	2	0	1092.4	1094.4
18	DN	2	2	2	0	1092.4	1094.4
19	DN	2	2	2	0	1092.4	1094.4
20	DN	2	2	2	0	1092.4	1094.4
21	R	3	1	2	12000	53.3	12055.3
22	DN	1	1	2	0	53.6	55.6
23	DN	1	1	2	0	53.6	55.6
24	DN	2	2	2	0	1092.4	1094.4
25	DN	2	2	2	0	1092.4	1094.4

## Alternative scenario

Year	Action	State before Action	State after Action	Monit. Cost kEuro	Maint. Cost kEuro	TTL Cost kEuro	Total Cost kEuro
1	DN	1	1	100	0	0.0	100.0
2	DN	1	1	4	0	0.0	4.0
3	DN	2	2	4	0	109.5	113.5
4	DN	2	2	4	0	109.5	113.5
5	DN	2	2	4	0	109.5	113.5
6	DN	2	2	4	0	109.5	113.5
7	DN	3	3	4	0	1460.0	1464.0
8	DN	3	3	4	0	1460.0	1464.0
9	DN	3	3	4	0	1460.0	1464.0
10	R	4	1	4	12000	0.0	12004.0
11	DN	1	1	4	0	0.0	4.0
12	DN	1	1	4	0	0.0	4.0
13	DN	2	2	4	0	109.5	113.5
14	DN	2	2	4	0	109.5	113.5
15	DN	2	2	4	0	109.5	113.5
16	DN	2	2	4	0	109.5	113.5
17	DN	3	3	4	0	1460.0	1464.0
18	DN	3	3	4	0	1460.0	1464.0
19	DN	3	3	4	0	1460.0	1464.0
20	R	4	1	4	12000	0.0	12004.0
21	DN	1	1	4	0	0.0	4.0
22	DN	1	1	4	0	0.0	4.0
23	DN	2	2	4	0	109.5	113.5
24	DN	2	2	4	0	109.5	113.5
25	DN	2	2	4	0	109.5	113.5

TOMORROW'S ROAD INFRASTRUCTURE MONITORING & MANAGEMENT

# Conclusions



- ▶ CBA: method based on Markov Decision process for maintenance planning
- ▶ SCBA: Extensions with respect to direct and indirect costs (social costs)
- ▶ Monitoring data: condition values and transitions (degradations)
- ▶ NPV's for comparing added value of monitoring systems
- ▶ Feasible method, although laborious
- ▶ Connecting: data ↔ information ↔ condition ↔ performance ↔ decisions ↔ actions
- ▶ Added value<sup>+</sup> : operational maintenance planning
- ▶ Further need of performance models